

Test - Gleichungen lösen

Name: \_\_\_\_\_

1. Löse die Gleichungen - gib die Lösungsmenge an.

$$G = \{ \dots, -2, -1, 0, 1, 2, 3, \dots \}$$

a)  $8+4x=6x-12$

$$\begin{array}{rcl} 8 & = & 2x - 12 \\ \underline{-4x} & & \underline{+12} \\ 20 & = & 2x \quad | :2 \\ x & = & 10 \\ \hline L & = & \{10\} \end{array}$$

b)  $(x-4)(x+1)=(x-2)(x-3)$

$$\begin{array}{rcl} x^2 + x - 4x - 4 & = & x^2 - 3x - 2x + 6 \quad | -x^2 \\ -3x - 4 & = & -5x + 6 \quad | +5x \\ 2x - 4 & = & 6 \quad | +4 \\ 2x & = & 10 \quad | :2 \\ x & = & 5 \quad L = \{5\} \end{array}$$

c)  $(x-2)^2=(x+6)^2$

$$\begin{array}{rcl} x^2 - 4x + 4 & = & x^2 + 12x + 36 \quad | -x^2 \\ -4x + 4 & = & 12x + 36 \quad | +4x \\ 4 & = & 16x + 36 \quad | -36 \\ -32 & = & 16x \quad | :16 \\ x & = & -2 \quad L = \{-2\} \end{array}$$

d)  $x(x+5)=(x+2)^2$

$$\begin{array}{rcl} x^2 + 5x & = & x^2 + 4x + 4 \quad | -x^2 \\ 5x & = & 4x + 4 \quad | -4x \\ x & = & 4 \\ \hline L & = & \{4\} \end{array}$$

Datum: \_\_\_\_\_

2. Korrigiere den Fehler in jeder Aufgabe und rechne sie richtig zu Ende.

a)  $(x-4)(x-6)=(x+2)(x-8)$

$$\begin{array}{rcl} x^2 - 6x - 4x + 24 & = & x^2 - 8x + 2x - 16 \quad | -x^2 \\ x^2 - 10x + 24 & = & x^2 - 6x - 16 \quad | -x^2 \\ -10x + 24 & = & -6x - 16 \quad | +6x \\ -4x + 24 & = & -16 \quad | +24 \\ -4x & = & -40 \quad | :4 \\ x & = & +10 \quad | :(-4) \end{array}$$

b)  $(x-2)^2=(x+5)^2$

$$\begin{array}{rcl} x^2 - 4x + 4 & = & x^2 + 10x + 25 \quad | -x^2 \\ -4x + 4 & = & 10x + 25 \quad | +4x \\ 4 & = & 14x + 25 \quad | -25 \\ -21 & = & 14x \quad | :14 \\ -1,5 & = & x \end{array}$$

c)  $x(x-8)=(x-5)(x-6)$

$$\begin{array}{rcl} x^2 - 8x & = & x^2 - 6x - 5x + 30 \quad | -x^2 \\ x^2 - 8x & = & x^2 - 11x + 30 \quad | -x^2 \\ -8x & = & -11x + 30 \quad | +11x \end{array}$$

$$\begin{array}{rcl} +3x & -3x & = 30 \quad | :(-3) \quad | :3 \\ x & = & +10 \end{array}$$